

Show All work!

1) Simplify and Classify by degree and number of terms. A. $(-8d^3 - 7) - (-d^3 - d^2 - 6)$

$$-8d^3 - 7 + d^3 + d^2 + 6$$

$$-7d^3 + d^2 - 1$$

B. $x(x - 3) - 2x(x - 3)$

Cubic Eq.

$$x^2 - 3x - 2x^2 + 6x$$

$$-x^2 + 3x \quad \text{Quad B.}$$

2) Write a polynomial function in **standard form** with the roots $0, \frac{-2}{5}, 3$

$$y = x(x - 3)(5x + 2)$$

$$y = x(5x^2 - 13x - 6)$$

$$y = 5x^3 - 13x^2 - 6x$$

3) Solve to find all the roots. $x^3 - 64 = 0$

$$(x - 4)(x^2 + 4x + 16) = 0$$

$$x = 4$$

$$x^2 + 4x + 4 = -16 + 4$$

$$(x + 2)^2 = -12$$

$$x + 2 = \pm 2i\sqrt{3}$$

$$-2 \pm 2i\sqrt{3}$$

4) Solve to find all the roots. $8x^3 - 1 = 0$

$$(2x - 1)(4x^2 + 2x + 1) = 0$$

$$x = \frac{1}{2}$$

$$x = \frac{-2 \pm \sqrt{4 - 4(4)(1)}}{2(4)} = \frac{-2 \pm \sqrt{-12}}{8}$$

$$x = \frac{-2 \pm 2i\sqrt{3}}{8}$$

$$x = \frac{-1 \pm i\sqrt{3}}{4}$$

5) Divide using synthetic division.

$$(x^4 - 6x^2 - 27) \div (x + 2)$$

$$\begin{array}{r|rrrrr} -2 & 1 & 0 & -6 & 0 & -27 \\ & & -2 & 4 & 4 & -8 \\ \hline & 1 & -2 & -2 & 4 & -35 \end{array}$$

$$x^3 - 2x^2 - 2x + 4 + \frac{-35}{x+2}$$

6) Divide using long division.

$$(7x^3 + 11x^2 + 7x + 5) \div (x^2 + 1) = 7x + 11$$

$$\begin{array}{r} 7x^3 + 11x^2 + 7x + 5 \\ -7x^3 \quad \downarrow \quad +7x \quad \downarrow \\ \hline 11x^2 + 0x + 5 \\ -11x^2 + 0x + 11 \\ \hline -6 \end{array}$$

$$-6$$

7) Solve to find all zeros.

$$f(x)x^3 - 6x^2 + 4x + 16$$

$$\{4, 1 \pm \sqrt{5}\}$$

$$\begin{array}{r} 4 \overline{) 1 - 6 \ 4 \ 16} \\ \underline{-4 \ 8 \ -16} \\ 1 \ -2 \ -4 \ 0 \end{array}$$

$$x^2 - 2x + 4 = 0$$

$$x^2 - 2x + \boxed{4} = 4 + 1$$

$$(x-1)^2 = 5$$

$$x = 1 \pm \sqrt{5}$$

$$x = 1 \pm \sqrt{5}$$

8) Solve to find all zeros.

$$f(x) = x^3 - 9x^2 + 28x - 30$$

$$\{3, 3 \pm i\}$$

$$\begin{array}{r} 3 \overline{) 1 - 9 \ 28 \ -30} \\ \underline{-3 \ 27 \ -30} \\ 1 \ -6 \ 10 \ 0 \end{array}$$

$$x^2 - 6x + 10 = 0$$

$$x^2 - 6x + \boxed{9} = -10 + \boxed{9}$$

$$(x-3)^2 = -1$$

$$x = 3 \pm i$$

$$x - 3 = \pm i$$

9) You want to make an open top box from cardboard. The original cardboard is 20 X 30. Find the maximum volume and the length of the cut. Round to the nearest hundredth.

$$V = ((20-2x)(30-2x))x$$

$$\text{Max Volume: } 1056.31 \text{ unit}^3$$

$$\text{Length: } 3.92 \text{ units}$$

10) Is $(x-3)$ a factor of $x^3 - 4x^2 + x + 6 = 0$? If so, find the remaining factors.

$$\begin{array}{r} 3 \overline{) 1 - 4 \ 1 \ 6} \\ \underline{-3 \ 3 \ 6} \\ 1 \ -1 \ -2 \ 0 \end{array}$$

$$x^2 - x - 2 = 0$$

$$(x-2)(x+1)$$

11) Solve: $x^4 - 12x^2 - 64 = 0$

$$\begin{array}{r} -64 \\ -12 \times 4 \end{array}$$

$$x^4 - 16x^2 + 4x^2 - 64 = 0$$

$$x^2(x^2 - 16) + 4(x^2 - 16) = 0$$

$$(x^2 + 4)(x^2 - 16) = 0$$

$$x^2 = -4$$

$$x^2 = 16$$

$$x = \pm 2i$$

$$x = \pm 4$$

12) Solve: $x^4 - x^2 - 72 = 0$

$$\begin{array}{r} -72 \\ -1 \times 8 \end{array}$$

$$x^4 - 9x^2 + 8x^2 - 72 = 0$$

$$x^2(x^2 - 9) + 8(x^2 - 9) = 0$$

$$(x^2 + 8)(x^2 - 9) = 0$$

$$x^2 = -8$$

$$x^2 = 9$$

$$x = \pm 2i\sqrt{2}$$

$$x = \pm 3$$

13) Find the discriminant and describe the roots of:

$$3x^2 + 2x - 8 = 0$$

$$\text{and } x^2 - 2x - 7 = 0$$

$$(2)^2 - 4(3)(-8)$$

$$(-2)^2 - 4(1)(-7)$$

$$100$$

$$-24$$

2 Real Rational Roots

2 Imaginary Roots

14) Solve by completing the square

$$x^2 - 6x - 15 = 0$$

$$x^2 - 6x + \boxed{9} = 15 + \boxed{9}$$

$$(x-3)^2 = 24$$

$$x-3 = \pm \sqrt{24}$$

$$x = 3 \pm 2\sqrt{6}$$